
An “ideal gas law” for international diffusion of solar power?

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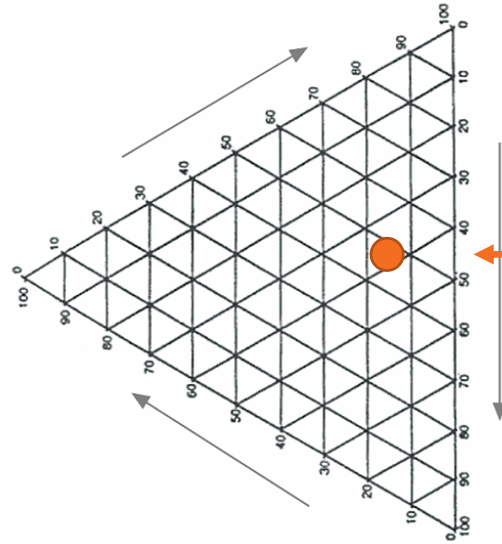
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Perspectives on model validation & uncertainty

1. Don't care
2. Accept inevitability



Empirical: explain most data with fewest free parameters

Self-identify: emphasis on reducibility, very little on completeness

Theoretical: Combination of

1. Reducibility,
2. Completeness,
3. Social validation

1. **Reducibility:** extent to which model can be reduced/derived from smaller set of principles or assumptions.
2. **Completeness:** # of influence factors accounted for.
3. **Social validation:** what your research community thinks is best practice.

Information Technology and Modeling



- IT enables dramatic progress on completeness of models
- Have to explore power of IT, but also... history of progress has been from dramatic simplifications of complex systems, not completeness
- Important to continue search for minimalistic, empirically robust models

PV Diffusion Modeling



- Long history of prior work
- Approaches: Bass model, Agent based, Fuzzy logic, Multi-variable regression
- Increasingly temporally and spatially resolved datasets for variables (prices, home suitability, demographics, ...)

Approach: Start simple, check empirics



- To predict: annual residential PV adoption per million detached houses (normalizing makes intrinsic variable)
- Start with ***one dependent variable***: Net Present Value as experienced by homeowners in region in that year.
- Collect data for multiple states/countries.
- Empirical check: is there a pattern?

Data collection

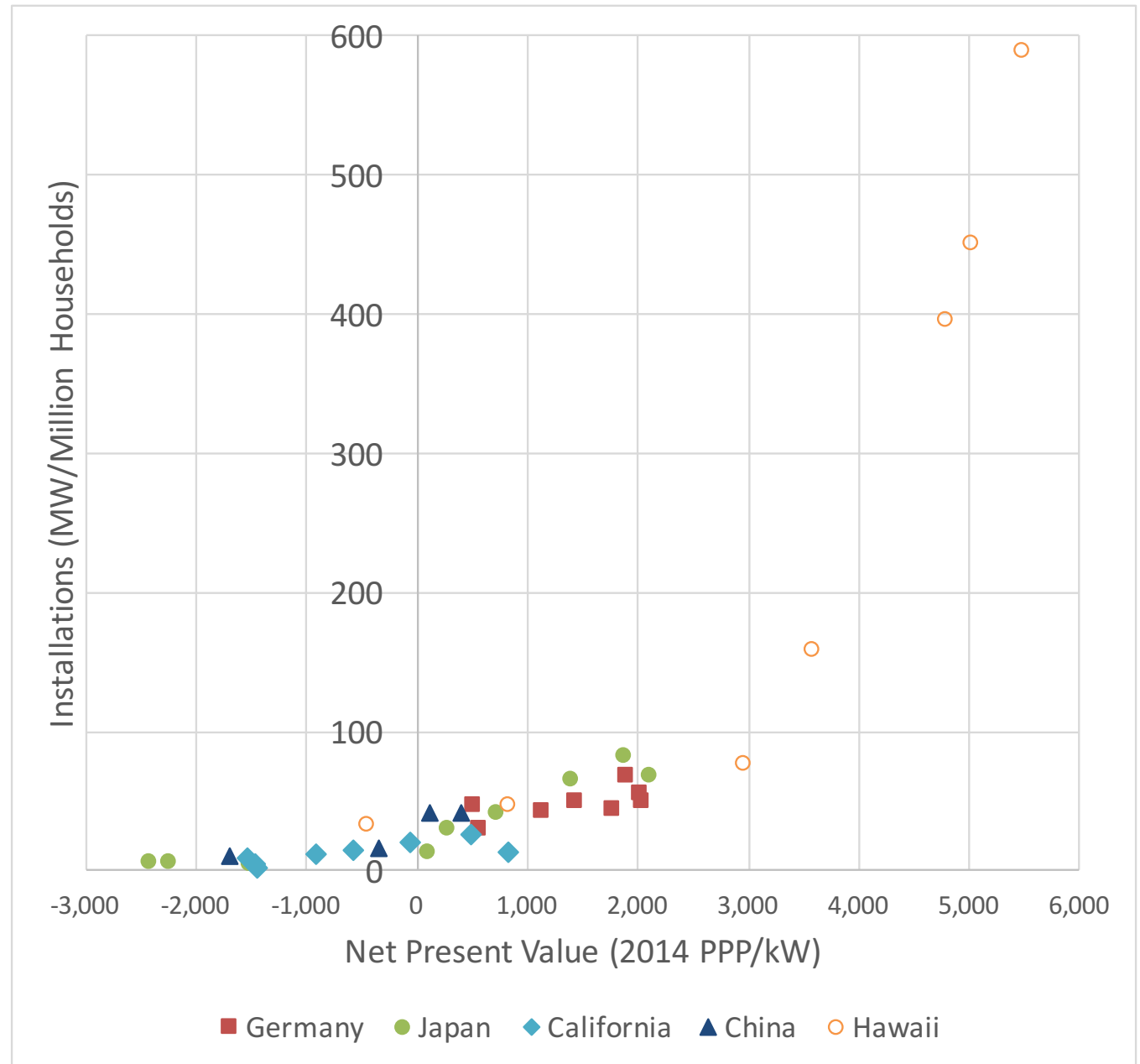


Find all data needed to calculation adoption and NPV in five regions: Japan, California, China, Germany and Hawaii, 2007-2014

Region	PV cost	Electricity price	Subsidies		Residential adoption	Detached Households
California	2007-2014 (IEA-PVPS 2014)	2007-2014 (EIA-CEP 2014)	2007-2014 (CSS 2017)		2007-2014 (CSS 2017)	2007-2014 (USCB 2000)
China	2011-2014 (IEA-PVPS-AR 2014)	2011 (CCTV-2011) 2012 (EPC-2012-2015)	2011 (IEA-PM, China) 2012 (IEA-PVPS-China 2012-2015)		2011-2014 (IEA-PVPS-China 2014)	2011-2014 (CICC 2015)
Germany	2007-2014 (IEA-PVPS Germany 2014)	2007-2014 (BDEW 2017)	2007-2014 (IEA-PVPS-AR 2014)		2007-2014 (Fraunhofer 2016)	2007-2014 (DSB 2017)
Hawaii	2008-2014 (IEA-PVPS 2014)	2008-2014 (EIA-HEP 2014)	2008-2014 (NC CETC 2015)		2008-2013 (IREC 2009-2014) 2014 (SEIA 2014)	2008-2014 (USCB 2000)
Japan	2007-2008 (METI 2013) 2009-2014 (JPEA -1 2014)	2007-2014 (METI-SEP)	FIT: 2010-2012 (Muhammad-Sukki et al 2014) 2013-2014 (IEA-PM, Japan)	Subsidy/tax credit: 2007-2008 (NEDO) 2009-2014	2007-2014 (JPEA-2 2014)	2007-2014 (MIAC-2013)

Result: Annual Installation vs. NPV

- Converted all currencies to 2014 Purchase Power Parity \$
- Surprisingly tight correlation



Adoption rate example: Japan in 2010



- 862 MW of residential PV installed in 2010 (JPEA).
- Assume potential adopters = number of detached homes = 29 million
- Adoption rate = 30 MW/million households in 2010.

Net Present Value (NPV)

$$NPV^j \left(\frac{\$}{kW} \right) = (-C_{total}^j + S^j) + \sum_{i=1}^N \frac{E^j * P_i^j}{(1 + int)^i}$$

- j is a year in a given region.
- C_{total}^j is investment cost of the PV system in year j
- S^j is investment subsidy in year j
- E^j is annual electricity production of the PV system in region (based on one central location)
- N is the lifetime of the system =20 years.
- P_i^j is displaced electricity price, FIT price or retail price in net metering region
- int , is the 10-year moving average of long-term interest rate less inflation

Net Present Value

Example: Japan in 2010

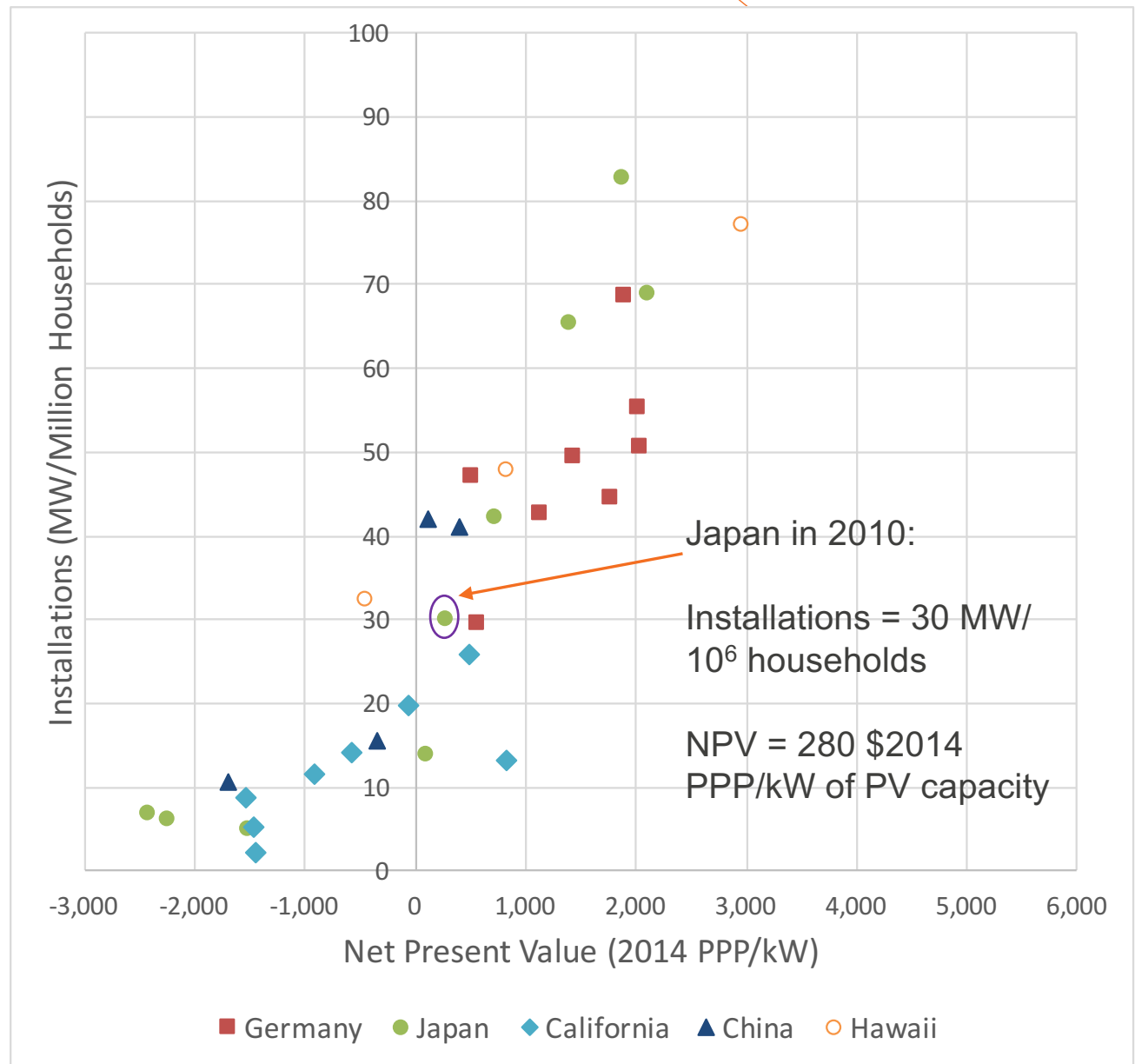


- PV installed price = 584 yen/Watt
- Electricity price = 20 yen/kWh
- Feed-in-tariff (1st 10 yrs) = 48 yen/kWh
- Annual generation of 3.9 kW system in Tokyo = 4,500 kWh
- Self consumption = 45%
- *Assume* retail price net metering for years 11-20
- $NPV_{2010} = 28,000 \text{ yen/KW} = 280$
\$2014 PPP

Zooming in on 0-100 MW/million household



Magnification reveals spread, but still good correlation



Explaining correlation with model

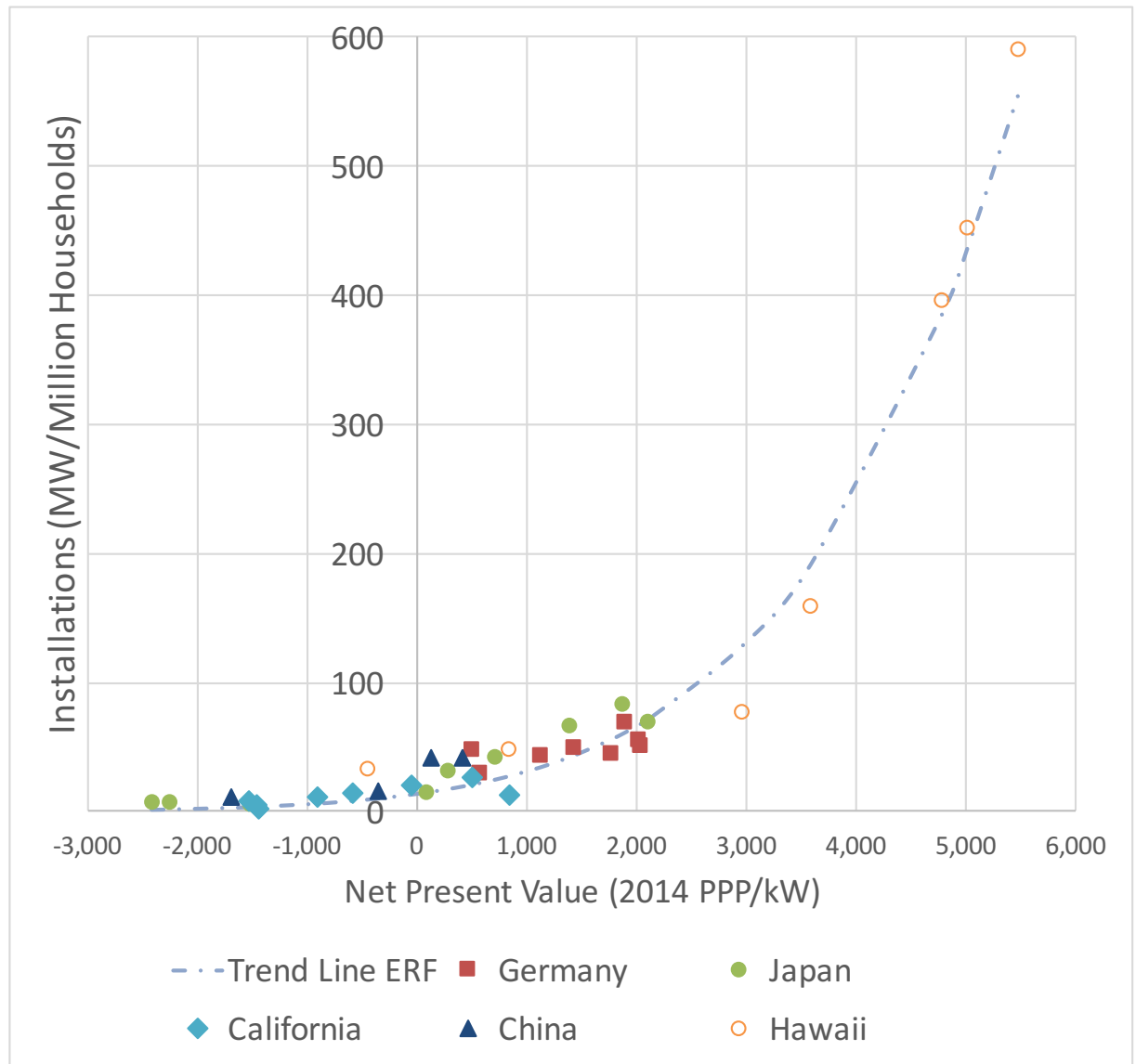
- Assume new PV customers added with increased NPV follows normal distribution.
- Adoption at given NPV:

$$\begin{aligned} \text{Annual adoption} \left(\frac{\text{MW}}{\text{million hh}} \right) (\text{NPV}) &= \alpha \int_{-\infty}^{\text{NPV}} dx e^{-\left(\frac{x-\mu}{\sigma}\right)^2} \\ &= \bar{\alpha} \left(1 + \text{erf} \left(\frac{\text{NPV} - \mu}{\sigma} \right) \right) \end{aligned}$$

- erf (x) is the error function,
- $\bar{\alpha}$ is a constant that can be fixed at 4,000 MW/million households (hh)
- μ is the peak customer acquisition value
- σ is the spread (variability in preferences)

Nonlinear regression results

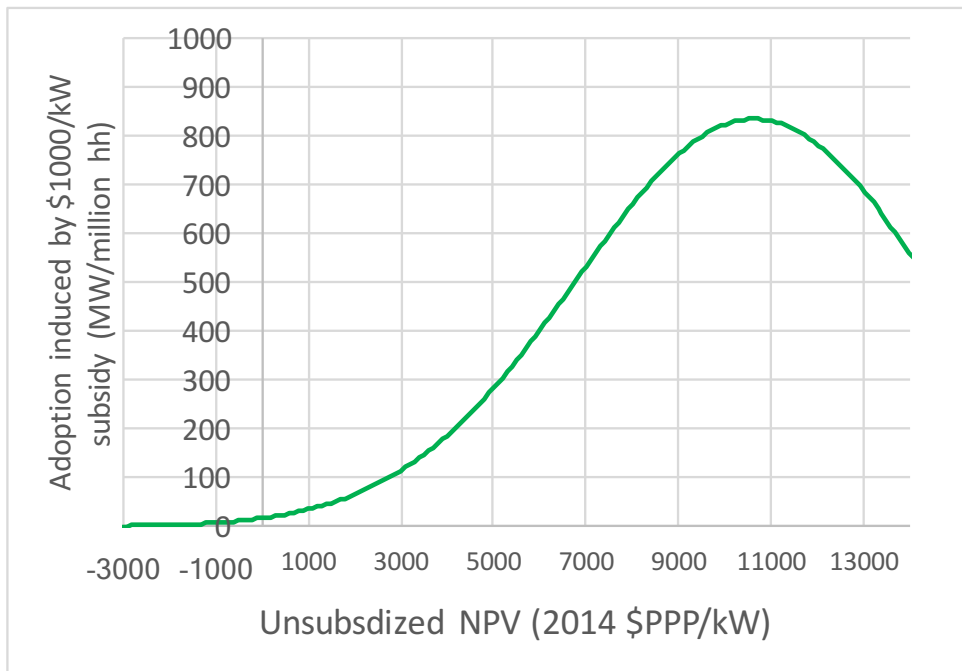
- $\mu = \$11,110$
\$/kW
- $\sigma = \$5,400$
\$/kW
- total square error (TSE) = 9,574.
- “Ideal Gas Law” for PV diffusion?



Application: Subsidy effectiveness

- Due to spread in consumer preferences, there are some consumers at (almost) any price
- How much adoption can be attributed to a subsidy?

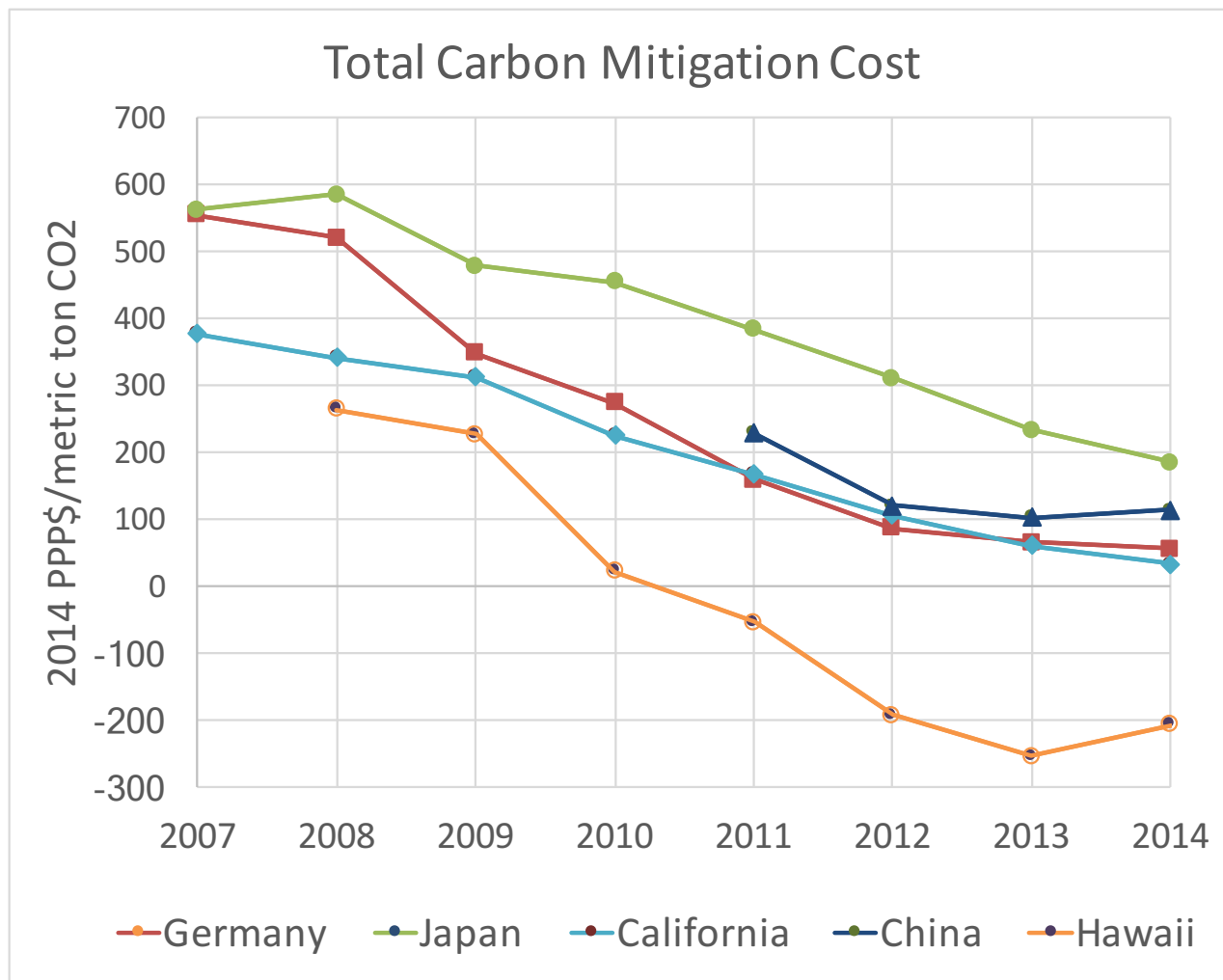
$$\text{Subsidy induced adoption} \left(\frac{\text{MW}}{\text{million hh}} \right) \\ = \text{Adoption (NPV with subsidies)} - \text{Adoption (NPV no subsidies)}$$



Subsidy is more effective for higher NPV (up to a point)

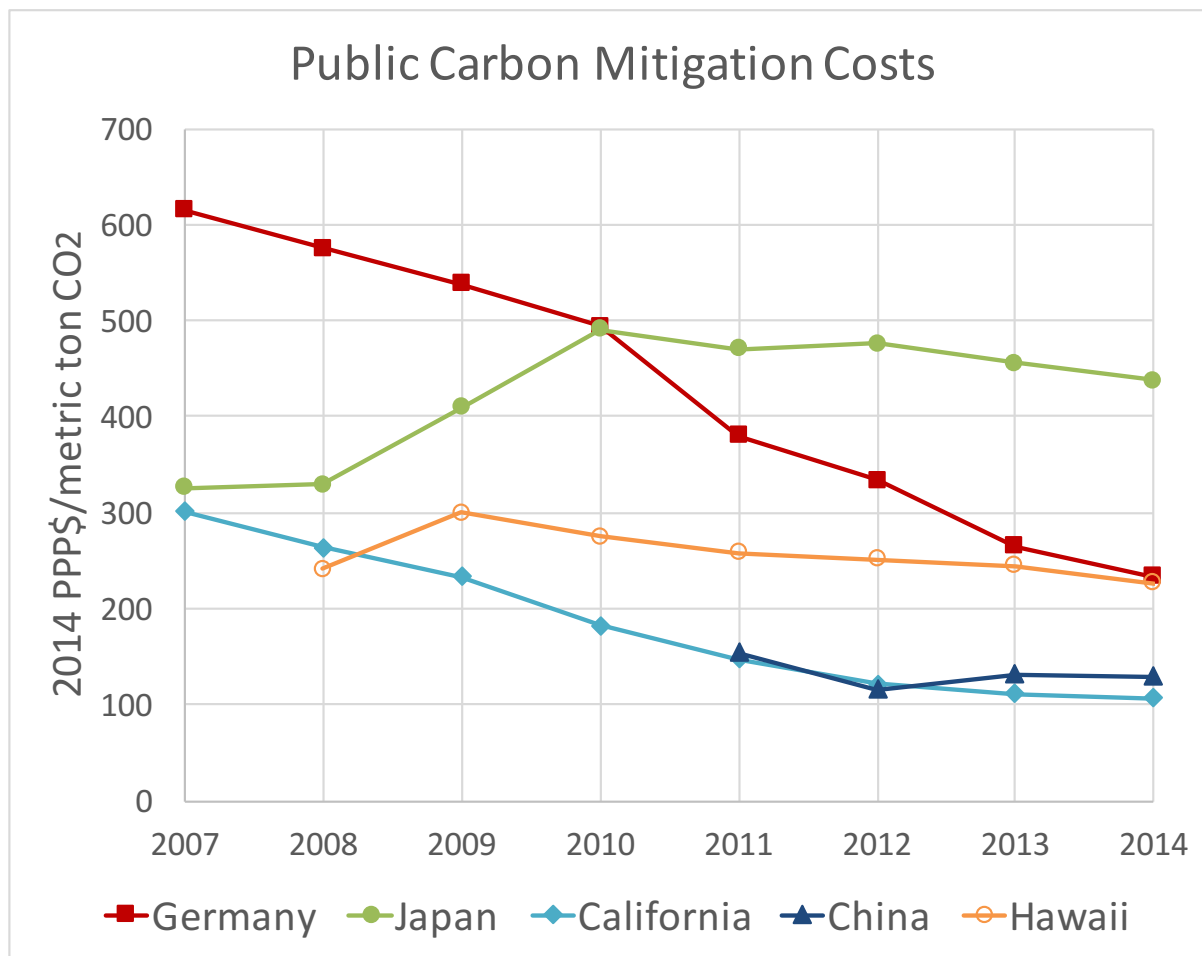
Application: total vs. public carbon mitigation costs

$$\text{Total Mitigation cost} \left(\frac{\$}{\text{ton } CO_2} \right) = \frac{\text{Total expenditures} (\$)}{\text{Total PV generation (MWh)} \times CO_2 \text{ reduction} \left(\frac{\text{tons } CO_2}{\text{MWh}} \right)}$$



Application: total vs. public carbon mitigation costs

$$\text{Public Mitigation Cost} \left(\frac{\$}{\text{ton } CO_2} \right) = \frac{\text{Subsidy Expenditures}(\$)}{\text{Subsidy induced PV generation (MWh)} \times CO_2 \text{ reduction} \left(\frac{\text{tons } CO_2}{\text{MWh}} \right)}$$



Improving the model

- More regions, years (note Hawaii is only region with high adoption)
- Divide into sub-regions (variations in irradiance, subsidies, prices)
- More explanatory variables (e.g. resale value, FIT vs. investment credit, purchase vs. lease)

Bigger picture: PV diffusion modeling and policy



- Subsidizing NPV **not** the only route to promote diffusion, also community solar, lease model, nudging, ...
- Bigger models needed to assess, e.g. agent-based, multivariable regression.

Thank you for your attention!



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